



Sharing

12 shared into 3 equal groups

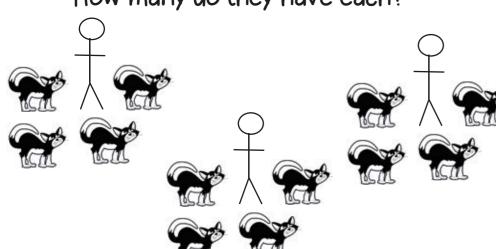
 $12 \div 3 = 4$

How many groups Grouping of 3 are there in 12?

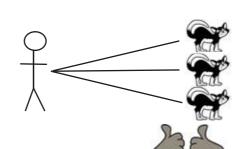
There are 12 cats. Each person owns 3 cats. How many people are there?

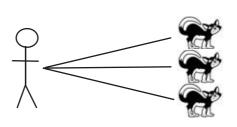
There are 12 cats.

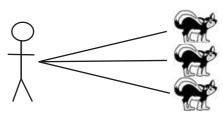
Three people each have the same number of cats. How many do they have each?



1 for you, 1 for you, 1 for you...

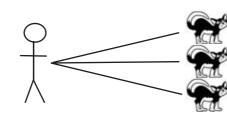




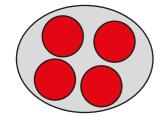


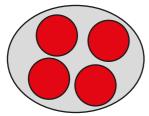
How shall I divide?

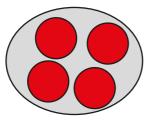


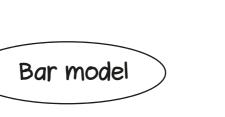


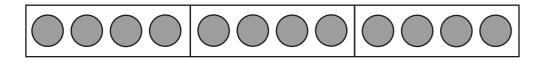
Grab a group of 3 grab a group of 3

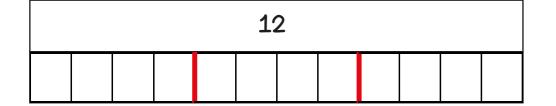


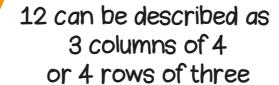


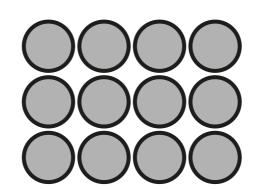


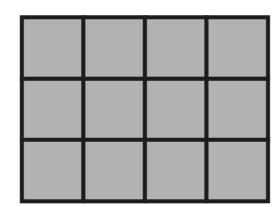


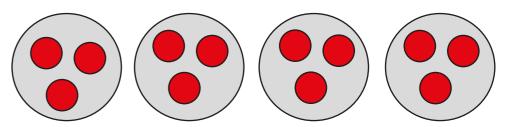




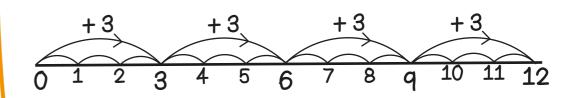
















8 + 7, 9 + 9, 14 + 3

Number facts

Single digit numbers

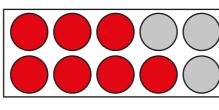
Doubles

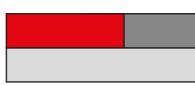
Teens and single digits

I just knew it!

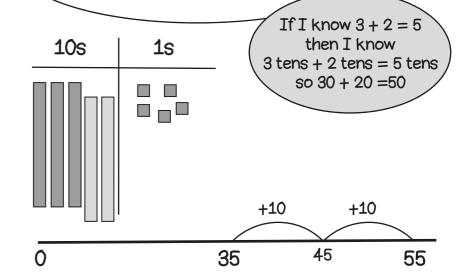
13 + 17 Use known facts 30 + 70

If I know 3 + 7 = 10 then I know 3 tens + 7 tens = 10 tens If I know 3 + 7 = 10 then I know 13 + 17 is 2 tens more





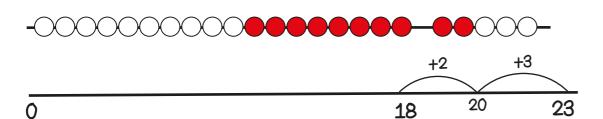
35 + 20 Add multiples of ten



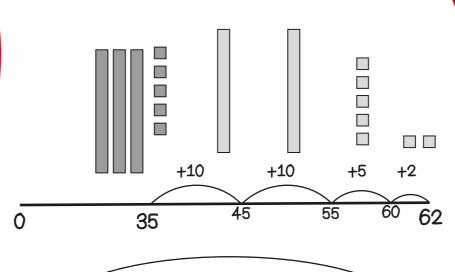
5 + 18 Greatest number first then bridge

25 + 43

Partition and recombine

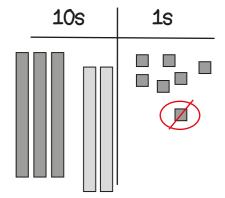


How shall I add?

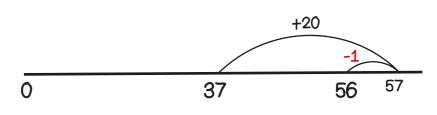


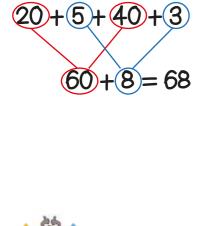
35 + 27 Count on in tens then ones

37 + 19 Round then adjust

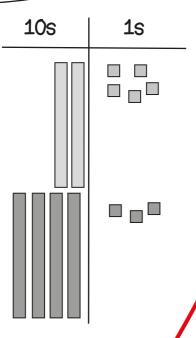


Add 20 then subtract 1





25 + 43

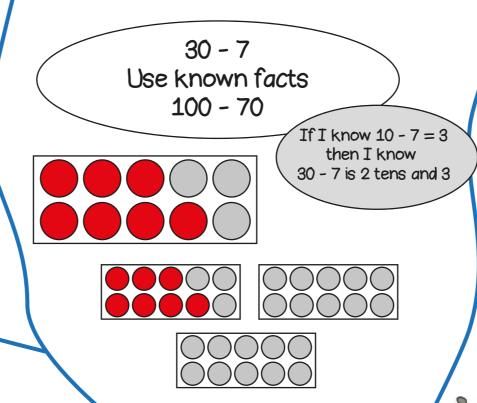




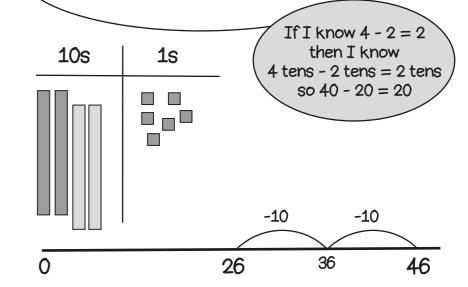
9 - 4, 13 - 5, 18 - 9 (Number facts Single digit numbers Halves Teens and single digits

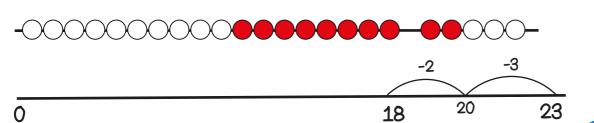
I just knew it!

23 - 5 Count back: bridge through a multiple of ten

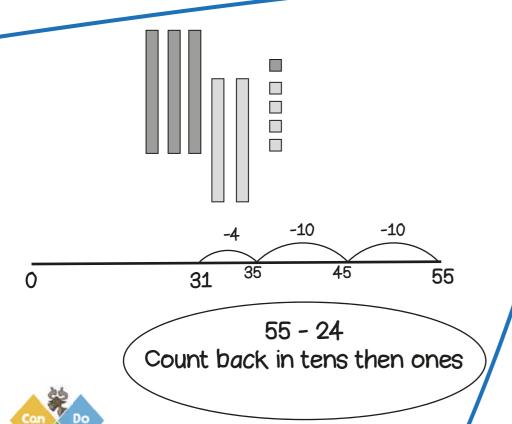


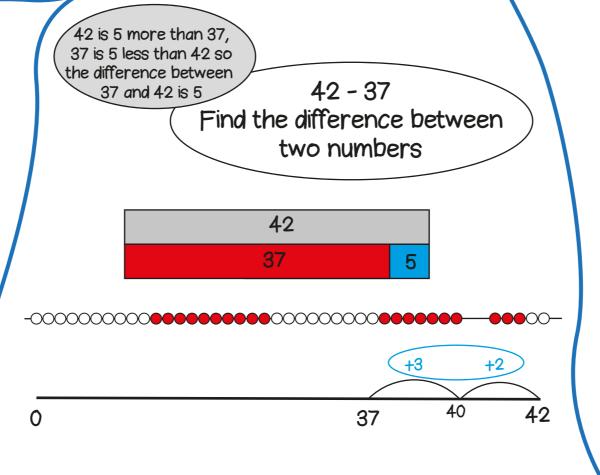
46 - 20 Count back: multiples of ten

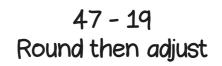


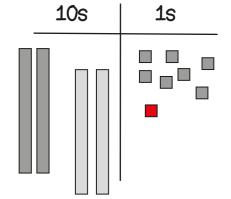


How shall I subtract?

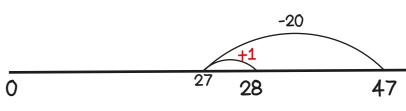






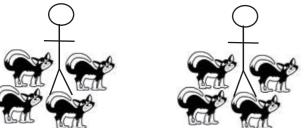


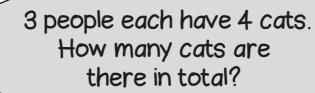
Take away 20 then add 1



Equal groups

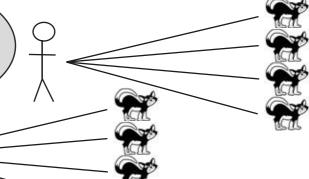
There are 3 groups with 4 cats in each group





One to many correspondence

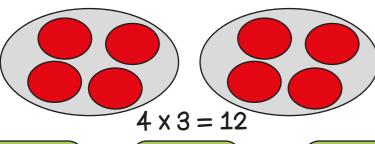
If each person has 4 cats, there are 4 times as many cats as people

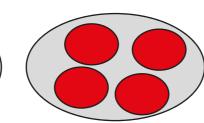


Recall of 2x, 5x and 10x tables



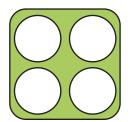
Four cats, multiplied by 3





People	Cats
1 2 3	4 8 12
	(









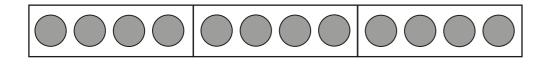
How shall I multiply?



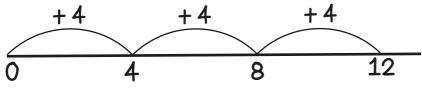








4	4	4
L A	L 1	± 1



$$4 + 4 + 4 = 12$$

Count in ones

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

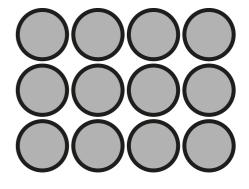
Count in twos

2, 4, 6, 8, 10,12

Use a known fact

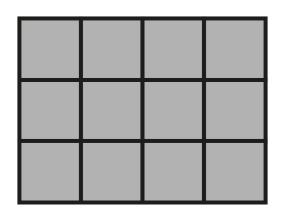
If 2 x 3 is 6, then 4 x 3 is double 6.





$$4 \times 3 = 12$$

$$3 \times 4 = 4 \times 3$$



Sharing

12 shared into 3 equal groups

 $12 \div 3 = 4$

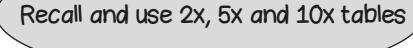
Grouping

How many groups of 3 are there in 12?

There are 12 cats.

Three people each have the same number of cats.

How many do they have each?

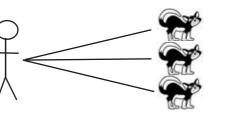


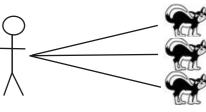
There are 12 cats. Each person owns 3 cats. How many people are there?



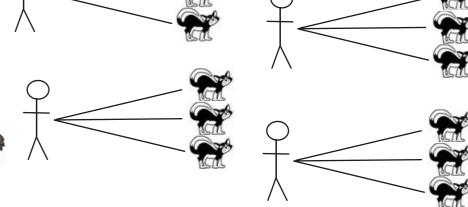
1 for you, 1 for you, 1 for you...

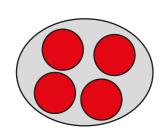
Grab a group of 3 grab a group of 3.

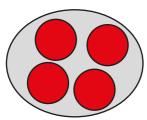


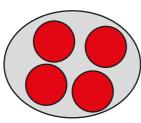




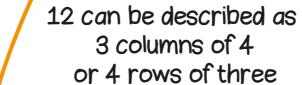


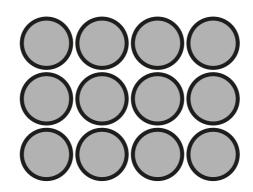


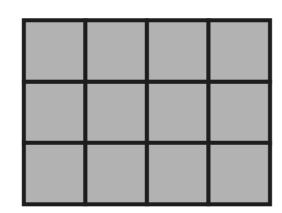




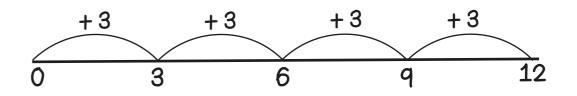
Bar model



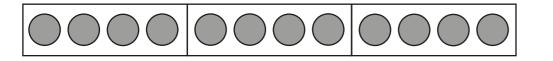








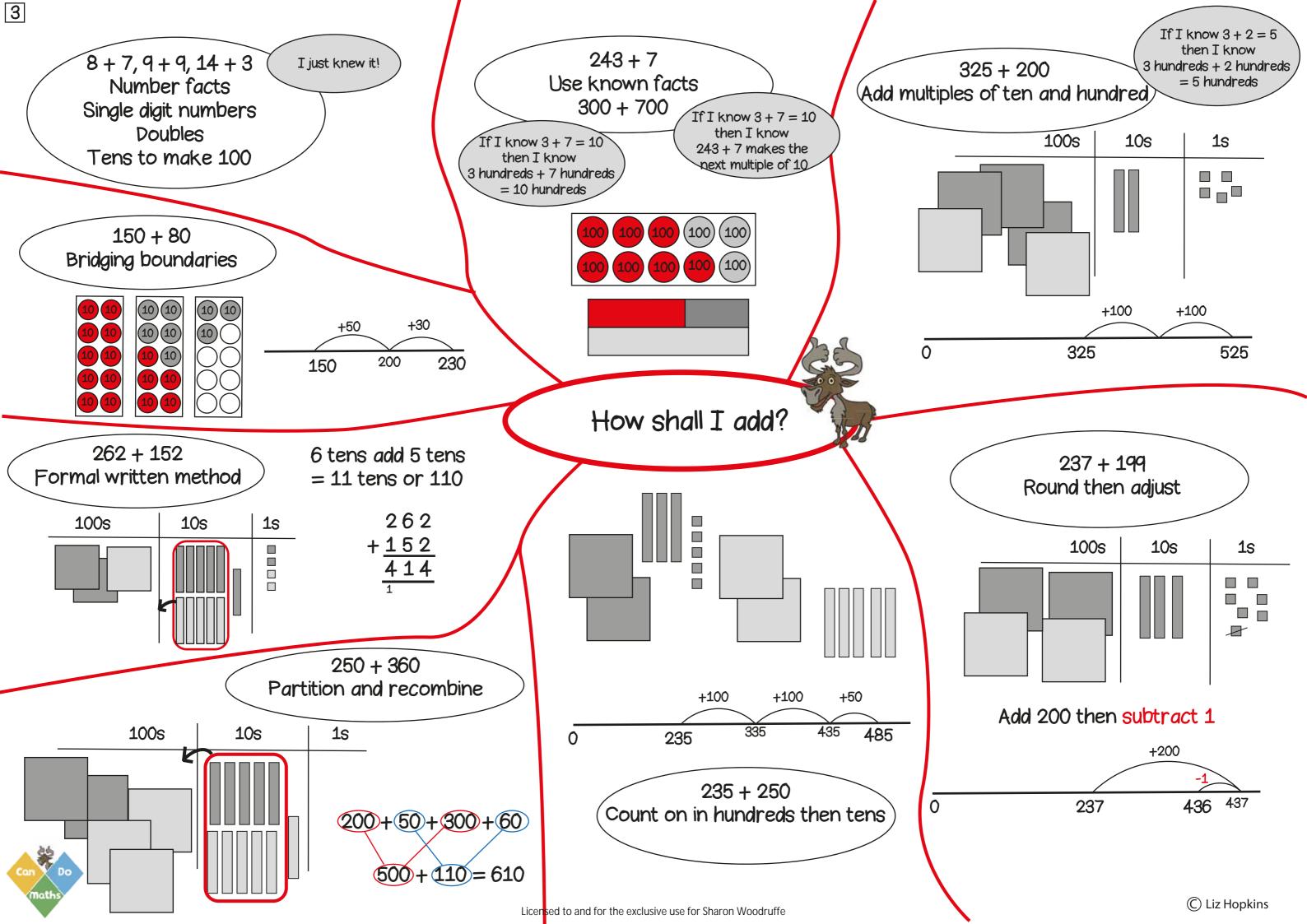
If I know $3 \times 4 = 12$ then I know $12 \div 3 = 4$



	12	
4	4	4

Link to fractions. One third of 12 is 4







15 - 8, 18 - 5 Number facts Single digit numbers Teens and single digits I just knew it!

240 - 7 Use known facts 1000 - 700

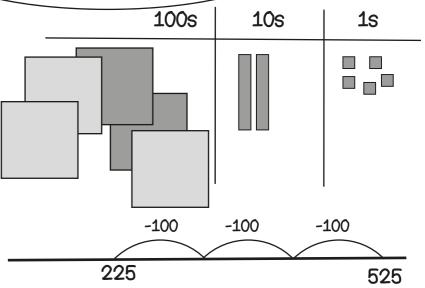
If I know 10 - 7 = 3then I know 10 hundreds - 7 hundreds = 3 hundreds



If I know 10 - 7 = 3then I know any multiple of 10, take away 7 leaves 3 in the ones.

525 - 300 Take away multiples of ten and a hundred

If I know 5 - 3 = 2then I know 5 hundreds - 3 hundreds = 2 hundreds



435 - 199

Round then adjust

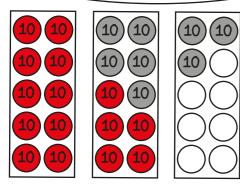
10s

1s

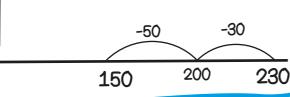
100s

Bridging boundaries by counting back in efficient steps

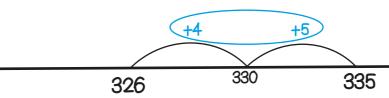
230 - 80



230 - 30 - 50 = 150

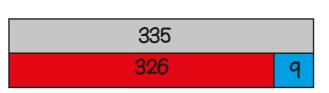


How shall I subtract?



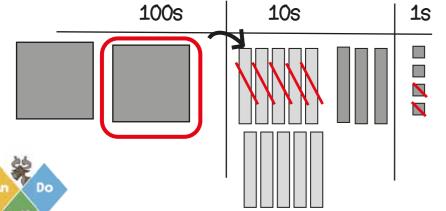
335 - 326 Find the difference between two numbers

> 335 is 9 more than 326 326 is 9 less than 335 so the difference between them is 9



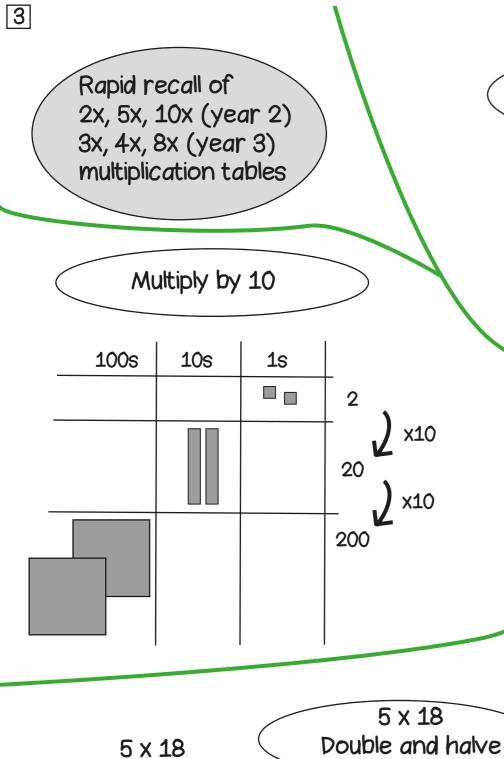
Formal written method ¹2 ¹3 4 -<u>152</u> 182 234 = 100 + 130 + 4100s 10s 1s

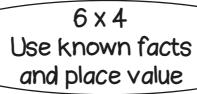
234 - 152



235 436 0 435

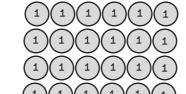
Take away 200 then add 1





$$6 \times 4 = 24$$

 $60 \times 4 = 240$
 $6 \times 40 = 240$



40 is ten times

greater than 4



 $=24\times10$

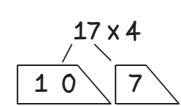
10

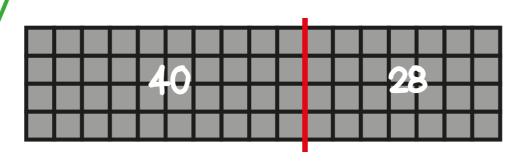
How shall I multiply?

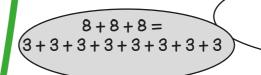
17 x 4 Partition and recombine

$$10 \times 4 + 7 \times 4$$

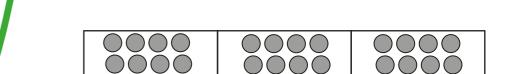
 $40 + 28 = 68$



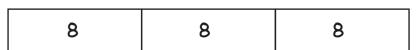


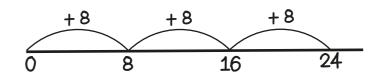


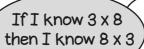
8 x 3 Repeated addition

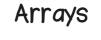


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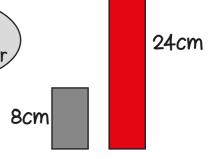












17 x 4 Formal written method

	10	7
4	40	28

17



 $= 5 \times 2 \times 18 \div 2$

10 x 9

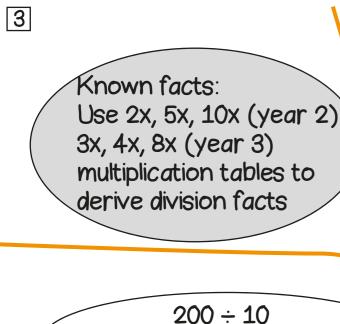
18

5

90

10

9



24 ÷ 4 Use known facts and place value

240 is ten times greater than 24

$$24 \div 4 = 6$$

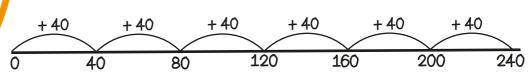
 $240 \div 40 = 6$
 $240 \div 4 = 60$

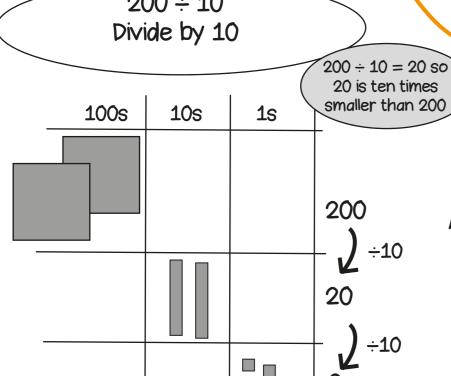
24 biscuits shared between 4 people means they will get 6 biscuits each.

If there are 10 times as many people and 10 times as many biscuits, how many biscuits each now?



 $240 \div 40 = 6$ How many steps of 40 make 240?



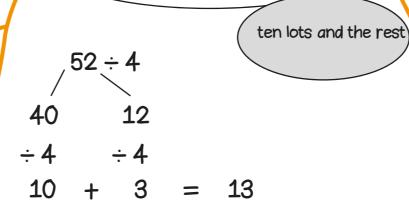


How shall I divide?

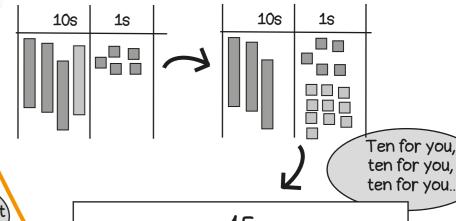
A tenth of is

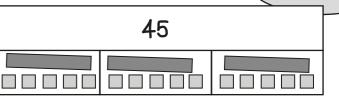
A tenth of 1 is 1 tenth so $1 \div 10 = \frac{1}{10}$

52 ÷ 4
Partition and recombine



45 ÷ 3 Sharing equally





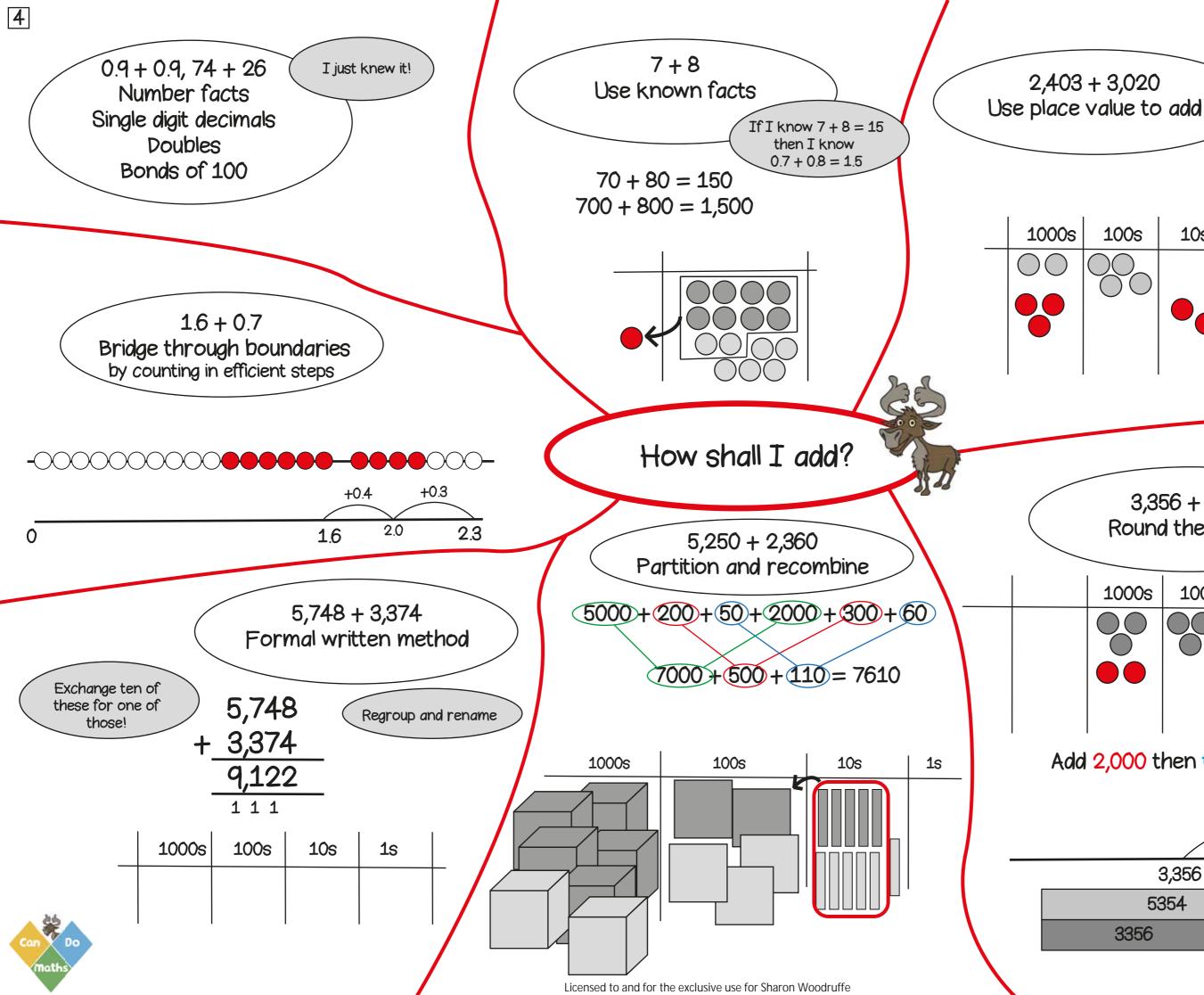
Link to fractions

42 ÷ 6 Double and halve If there are half as many biscuits and half as many people...

$$42 \div 6 = 21 \div 3$$

			42		
7	7	7	7	7	7
21					
7	7	7			
h.f.	•		•		

10 x 4 3 x 4 0 40 52

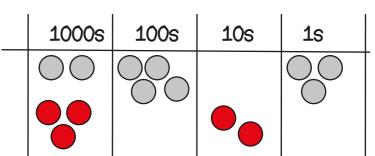


2,403 + 3,020

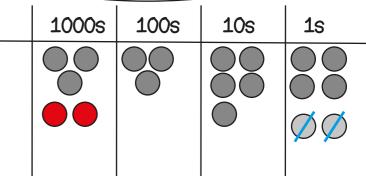
I have noticed, one number has no hundreds or ones, the other has no tens

If I know 2+3=5then I know

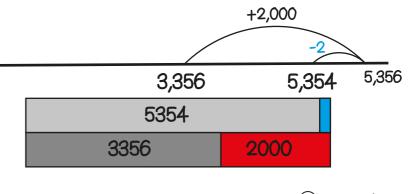
2000 + 3000 = 5000



3,356 + 1,998 Round then adjust



Add 2,000 then take away 2



© Liz Hopkins

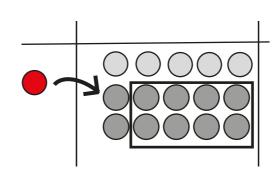
13 - 5, 1.8 - 0.8 Number facts Single digit numbers Halves Wholes and tenths

15 - 8 = 7Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

$$150 - 80 = 70$$

 $1500 - 800 = 700$



6,342 - 3,020 Use place value to subtract

1000s

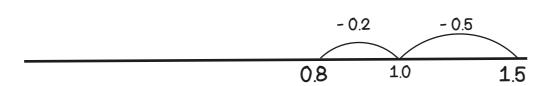
By using place value

1s

10s

counters it is easy to see how to take away

1.5 - 0.7Bridge through boundaries by counting in efficient steps



How shall I subtract?

5,352 - 2,136 Formal written method

I just knew it!

Exchange ten of these for one of those!

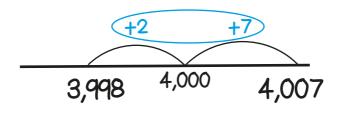
5,352 2,436

Regroup and rename

2,916

1000s	100s	10s	1 s	

4007-3998 Find the difference between two numbers



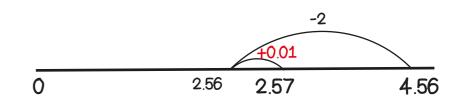
4,007 3,998

4.56 - 1.99 Round then adjust

100s

1 s	$\frac{1}{10}$ S	100 s

Take away 2 then add one hundredth







Known facts: Rapid recall of all multiplication tables up to 12 x 12

6 x 4 Use known facts and place value

 $6 \times 4 = 24$ $60 \times 4 = 240$



40 is ten times

greater than 4

10 10 10 10 10

 $60 \times 40 = 2400$

6x10x4x10

 $=24 \times 100$

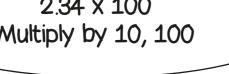
x10

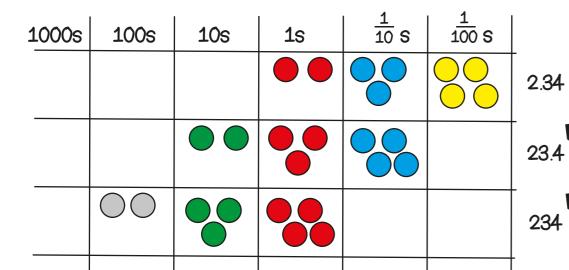
x10



10 10 10 10 10

2.34 x 100 Multiply by 10, 100

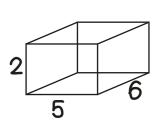




How shall I multiply?



7 x 36 Use the distributive law

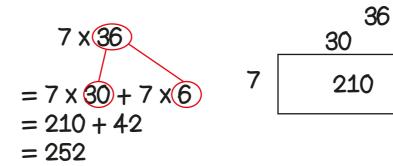


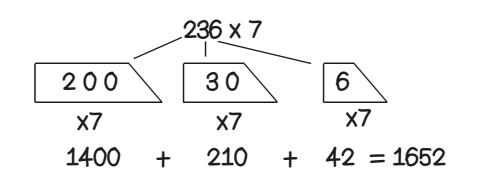
 $2 \times (5 \times 6) = (2 \times 5) \times 6$ $2 \times 30 = 10 \times 6$

45 x 6 $=5\times9\times6$ $=5\times6\times9$ $= 30 \times 9$ = 270

45 x 6 Use factors and commutativity



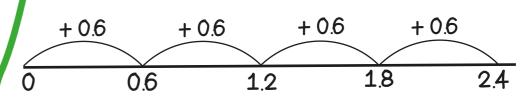




0.6 is ten times smaller than 6

6 x 4 Use known facts and place value

 $0.6 \times 4 = 2.4$ 4 jumps of 0.6



 $0.6 \times 4 = 24 \text{ tenths}$ $0.6 \times 4 = 2.4$

4

0.6

36 x 7 Formal written method

	30	6
7	210	42

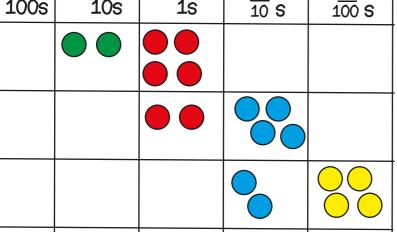
36

1



Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

> 24 ÷ 100 Divide by 10, 100



24 ÷ 4 Use known facts and place value

$$24 \div 4 = 6$$

 $240 \div 40 = 6$
 $2400 \div 400 = 6$

$$2400 \div 400 = \frac{24 \times 100}{4 \times 100}$$
$$\frac{24}{4} = 6$$

240 is ten times greater than 24

24 biscuits shared between 4 people means they will get 6 biscuits each.

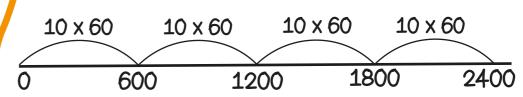
If there are 100 times as many people and 100 times as many biscuits, how many biscuits each now?

60 is ten times areater than 6

2400 ÷ 60 Use known facts and place value

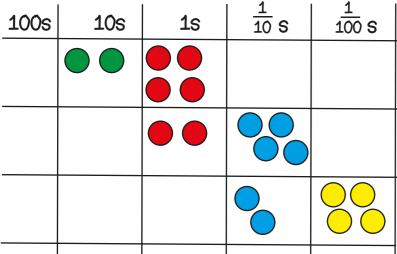
 $2400 \div 60 = 40$

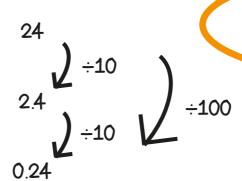
How many steps of 60 make 2400?



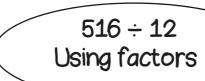
732 ÷ 6

Formal written method



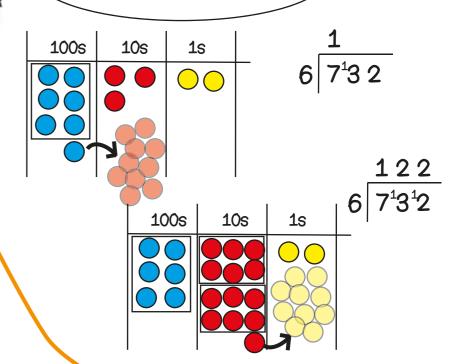


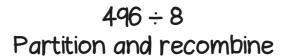
How shall I divide?

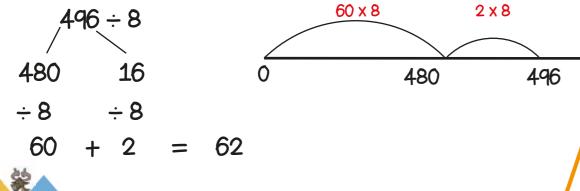


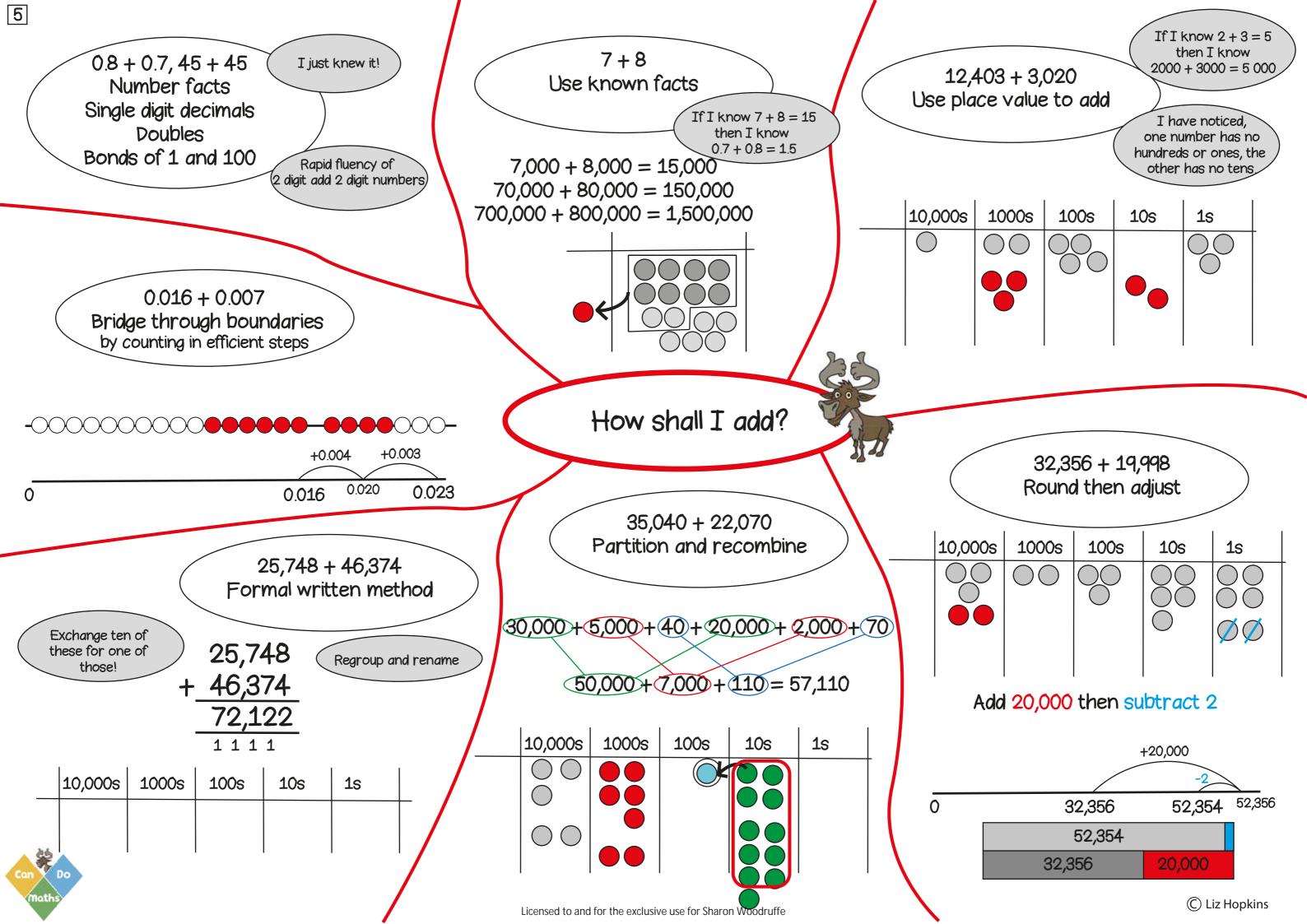
$$516 \div 3 \div 4$$

516											
172				172			172				
43	43	43	43								









9-4, 13-5, 18-9 Number facts Single digit decimals Halves Subtract from 1 and 100

I just knew it!

Rapid fluency of

2 digit subtract

2 digit numbers

Use known facts

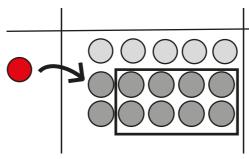
If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

15,000 - 8,000 = 7,000

15 - 8 = 7

150,000 - 80,000 = 70,000

1,500,000 - 800,000 = 700,000



Now it is easy to take away 3000

40,012 - 3,005 Use place value to subtract

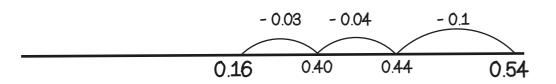
If I know 40 - 3 = 37then I know that 40 thousand take away 3 thousand is 37 thousand

5 less than 12 is 7

40,000 = 4 tens of thousands or 40 thousands 12 = 1 ten and 2 ones or 12 ones

40,012 = 40 thousands and 12 ones take away 3 thousands and 5 ones equals 37 thousands and 7 ones.

0.54 - 0.17Bridge through boundaries by counting in efficient steps

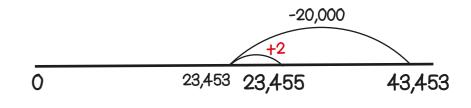


How shall I subtract?

43,453 - 19,998 Round then adjust

10,000s	1000s	100s	10 s	1s

Take away 20,000 then add 2



45,748 - 26,374 Formal written method

Exchange ten of these for one of those!

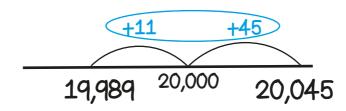
45,748

Regroup and rename

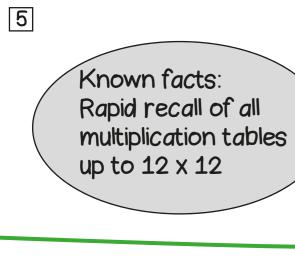
26,374 19,374

10,000s	1000s	100s	10 s	1 s

20,045 - 19,989 Find the difference between two numbers



20,045	
19,989	56



6 x 4 Use known facts and place value

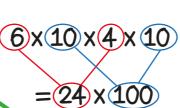
40 is ten times greater than 4











x10

x10

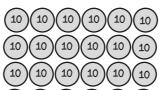
√ x10

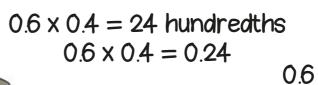
x100

 $6 \times 4 = 24$

 $60 \times 4 = 240$

 $60 \times 40 = 2400$





 $0.6 \times 4 = 2.4$

4 jumps of 0.6

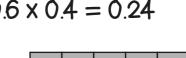
+ 0.6

0.6 is ten times

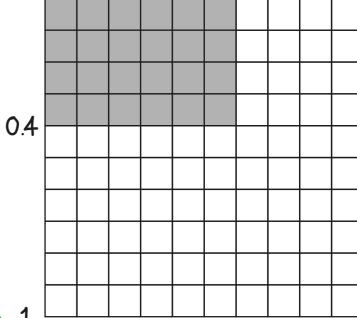
smaller than 6

0.6

+ 0.6



1.2



6 x 4

Use known facts

and place value

1.8

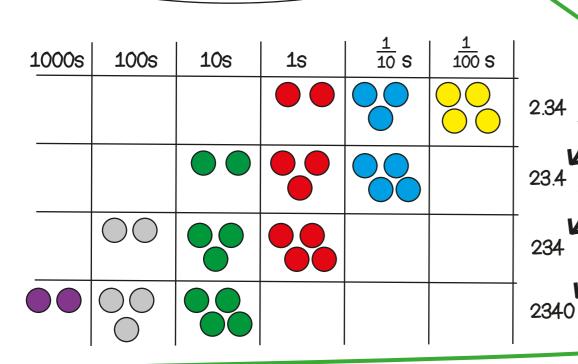
+ 0.6

2.4

1

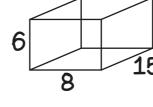
+ 0.6

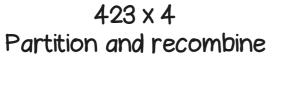
2.34 x 1000 Multiply by 10, 100, 1000

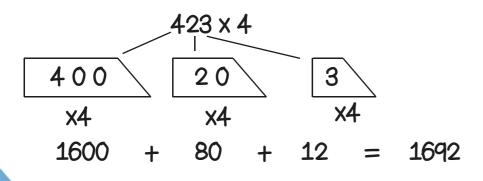


How shall I multiply?

15 x 42 Using factors and distributive law







15 x 14) $= 15 \times 6 + 15 \times 8$ = 90 + 120= 210

= 720

	427 x 38	3
Forma	l written	method

	400	20	7
30	12,000	600	210
8	3,200	160	56

427

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Include calcuations where remainders occur

24 ÷ 4

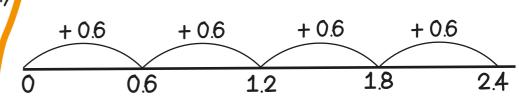
÷1000

Use known facts and place value 24,000 is a thousand times greater than 24

0.6 is ten times smaller than 6 2.4 ÷ 0.6 Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



5724 ÷ 4

Formal written method

24 ÷ 1000

Divide by 10, 100, 1000

Known facts:

Use recall of all

up to 12 x 12 to

multiplication tables

derive division facts

$$240 \div 40 = 6$$

 $2400 \div 400 = 6$
 $24,000 \div 4000 = 6$

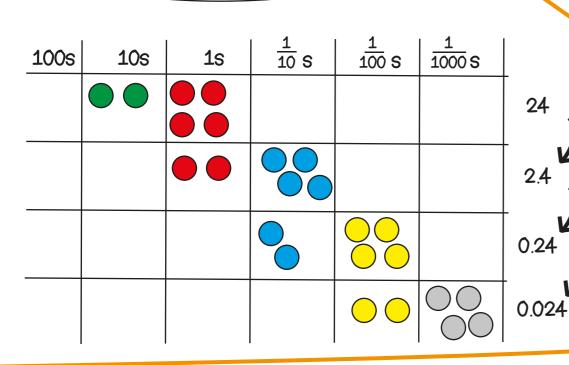
 $24 \div 4 = 6$

4 people means they will get
6 biscuits each.
If there are 1000 times as many
people and 1000 times as many
biscuits, how many biscuits
each now?

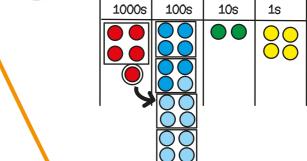
24 biscuits shared between

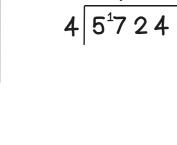
$$24,000 \div 400 = \underbrace{24 \times 1000}_{4 \times 100}$$
$$\underbrace{240}_{60} = 60$$

÷10



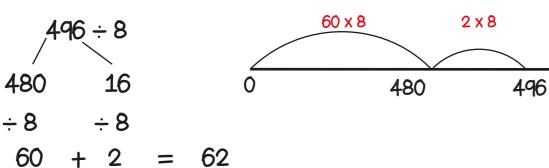
How shall I divide?





1000s 100s 10s 1s 1 4 5 1 7

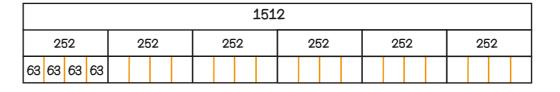
496 ÷ 8 Partition and recombine



1512 ÷ 6 ÷ 4

1512 ÷ 24

Using factors





44 + 56, 27 + 27 Number facts Single digit decimals Doubles Bonds of 1 and 100

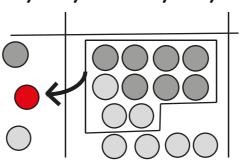
I just knew it!

Rapid fluency of 2 digit add 2 digit numbers 17 + 17 Use known facts

> If I know 17 + 17 = 34 then I know 1.7 + 1.7 = 3.4

17,000 + 17,000 = 34,000 170,000 + 170,000 = 340,000

1,700,000 + 1,700,000 = 3,400,000



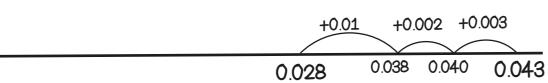
1,102,403 + 50,020 Use place value to add

I have noticed, one number has no hundreds or ones, the other has no tens

1,000,000s	100,000s	10,000s	1000s	100s	10 s	1 s
				00		

0.028 + 0.015 Bridge through boundaries by counting in efficient steps





325,748 + 246,374 Formal written method

Regroup and rename

Exchange ten of these for one of those!

0

325,748 + 246,374 572,122

100,000s	10,000s	1000s	100s	10 s	1 s	

How shall I add?

307,040 + 206,070 Partition and recombine

300,000 + 7,000 + 40 + 200,000 + 6,000 + 70

500,000 + 13,000 + 110 = 513,110

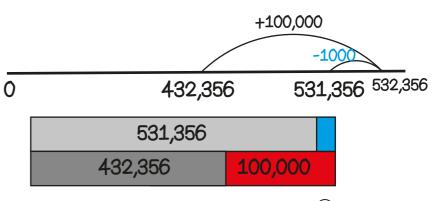
100,000s	10,000s	1000s	100s	10s	1 s	
00						Ī
1	l I					I

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432,356 + 99,000 Round then *adjust*

100,000s	10,000s	1000s	100s	10s	1 s
		Ø		000	000

Add 100,000 then take away 1,000



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0.9 - 0.4, 100 - 65 Number facts Single digit decimals Halves

I just knew it!

36 - 18 = 18Use known facts

400,032 - 30,005 Use place value to subtract

Bonds of 1 and 100

3.6 - 1.8 = 1.836,000 - 18,000 = 18,000

400,000 = 4 hundreds of thousands

Rapid fluency of 2 digit subtract 2 digit numbers

360,000 - 180,000 = 180,000 3,600,000 - 1,800,000 = 1,800,000

or 400 thousands 400 - 30 = 370 so 400,000 - 3,000 = 370,000

0.054 - 0.017 Bridge through boundaries by counting in efficient steps

400,032 = 400 thousands and 32 ones take away 30 thousands and 5 ones = 370,027

- 0.004 - 0.01 - 0.03 0.040 0.044 0.054 0.037

How shall I subtract?

If I know 36 - 18 = 18

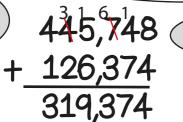
then I know

445,748 - 126,374 Formal written method

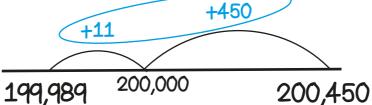
Regroup and rename

200,450 - 199,989 Find the difference between two numbers



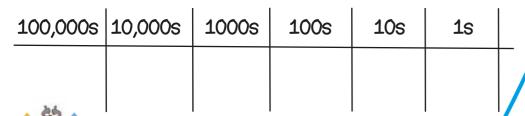


4 00



200,450 199,989

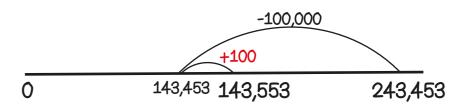
461



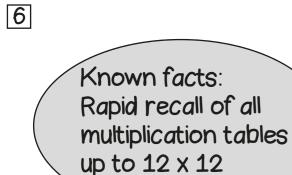
243,453 - 99,900 Round then adjust

	_					
100,000s	10,000s	1000s	100s	10s	1s	
	00				00	

Take away 100,000 then add 100



5 less than 32 is 27



6 x 4 Use known facts and place value

x10

x10

/ x10

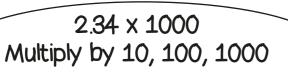
40 is ten times greater than 4

$$60 \times 40 = 2400$$

$$600 \times 400 = 240,000$$

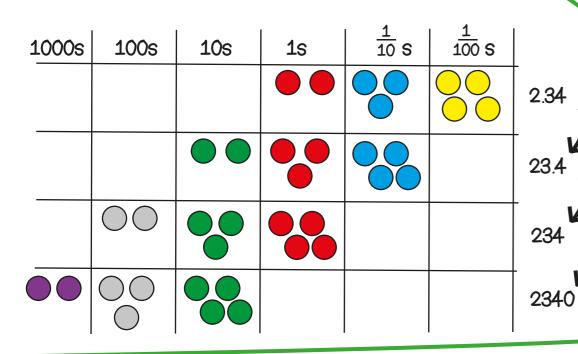
6x10x4x10

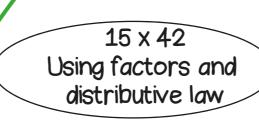
x100



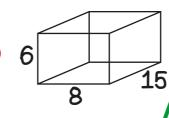


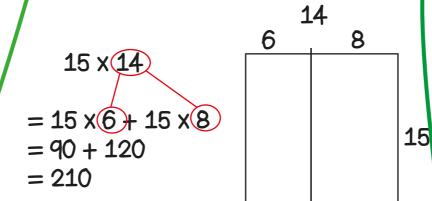
How shall I multiply?





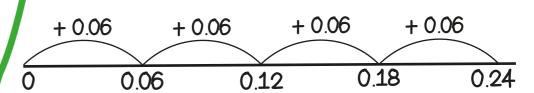
 15×48 = $15 \times 6 \times 8$ = 90×8



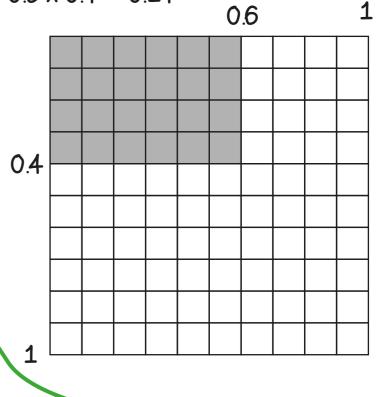


0.6 is ten times smaller than 6
Use known facts and place value

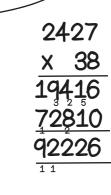
> $0.06 \times 4 = 0.24$ 4 jumps of 0.06



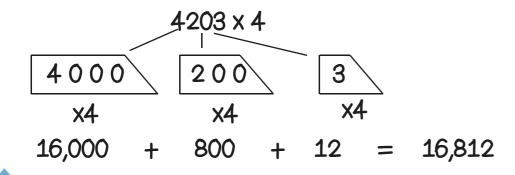
 $0.6 \times 0.4 = 24$ hundredths $0.6 \times 0.4 = 0.24$



2427 x 38 Formal written method



4203 x 4 Partition and recombine



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= 720

Known facts: Use recall of all multiplication tables up to 12 x 12 to

derive division facts

24 ÷ 1000

Divide by 10, 100, 1000

6

Include calcuations where remainders occur

24 ÷ 4

240 is ten times

Use known facts and place value

greater than 24

24 biscuits shared between 4 people means they will get

6 biscuits each.

If there are 10 times as many people and 10 times as many biscuits, how many biscuits

each now?

 $24,000 \div 4000 = 6$ $240,000 \div 40,000 = 6$ $2,400,000 \div 400,000 = 6$

÷10

 $240 \div 40 = 6$

 $2400 \div 400 = 6$

$$240,000 \div 400 = \underbrace{24 \times 10,000}_{4 \times 100}$$

$$\frac{2400}{4} = 600$$

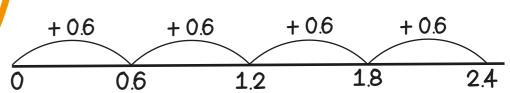
÷1000

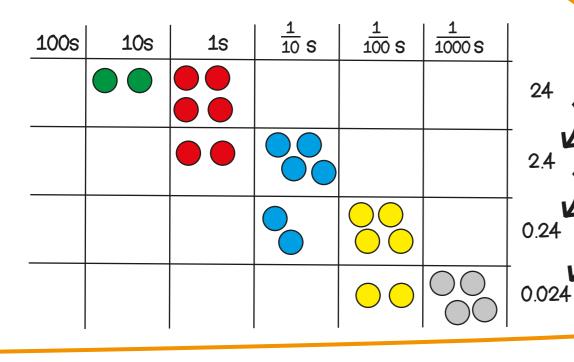
0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



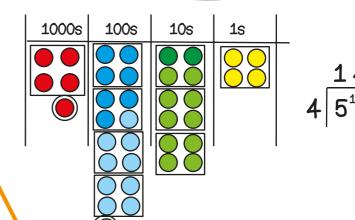


How shall I divide?

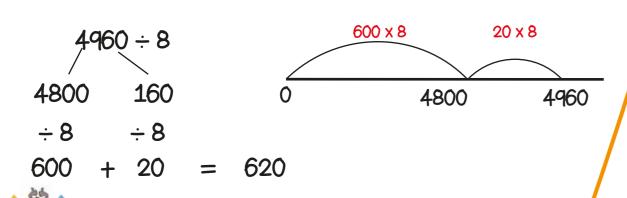
1512 ÷ 24

Using factors

7182 ÷ 21 Formal written method



4960 ÷ 8 Partition and recombine



 $1512 \div 6 \div 4$

	1512																						
	252				252			252			252			252			252						
4	63	63	63	63																			

342 7182 88